MATHCOUNTS®

2019 Mock Chapter Competition Sprint Round Problems 1–30

HONOR PLEDGE

I pledge to uphold the highest principles of honesty and integrity as a Mathlete*. I will neither give nor accept unauthorized assistance of any kind. I will not copy another's work and submit it as my own. I understand that any competitor found to be in violation of this honor pledge is subject to disgualification.

Signature _____ Date _____

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2

3

5

Printed Name

School

DO NOT BEGIN UNTIL YOU ARE INSTRUCTED TO DO SO.

This section of the competition consists of 30 problems. You will have 40 minutes to complete all the problems. You are not allowed to use calculators, books or other aids during this round. If you are wearing a calculator wrist watch, please give it to your proctor now. Calculations may be done on scratch paper. All answers must be complete, legible and simplified to lowest terms. Record only final answers in the blanks in the left-hand column of the competition booklet. If you complete the problems before time is called, use the remaining time to check your answers.

In each written round of the competition, the required unit for the answer is included in the answer blank. The plural form of the unit is always used, even if the answer appears to require the singular form of the unit. The unit provided in the answer blank is the only form of the answer that will be accepted.

Total Correct	Scorer's Initials



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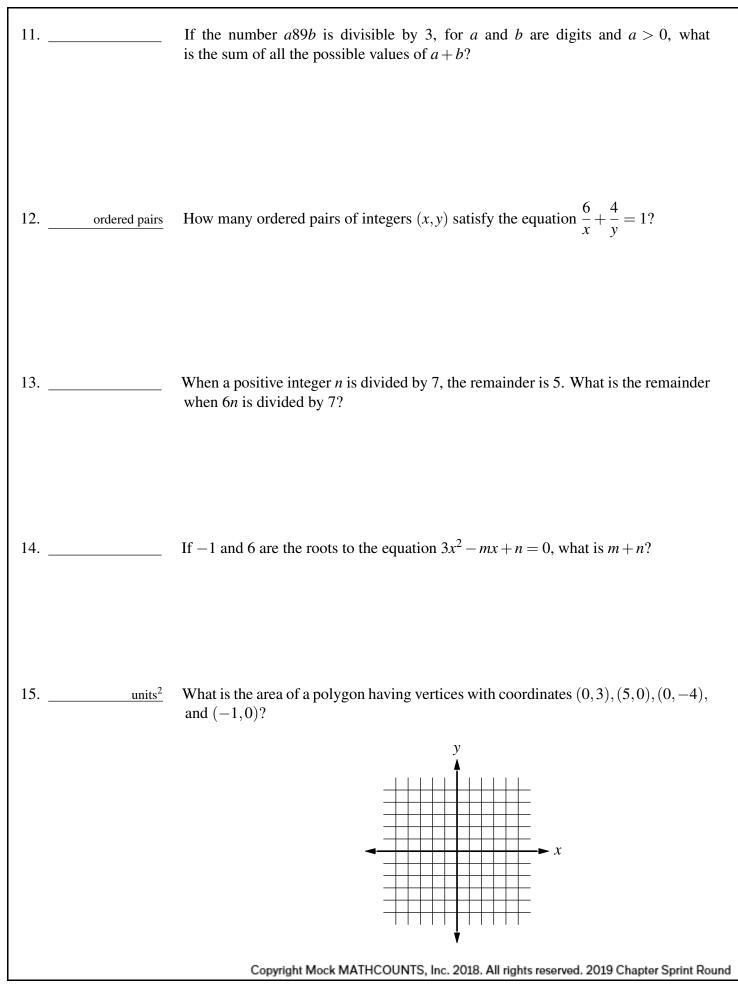
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1	What is the value resulted when the number fifty-four is subtracted from the number two thousand?
2	What is the sum of the two integers closest to the square root of 30?
3. <u>°F</u>	Absolute zero is the lowest possible temperature, which is approximately –459.7 °F. The boiling point of water is 212 °F. What is the sum of the boiling point of water and absolute zero? Express your answer as a decimal to the nearest tenth.
4 problems	Annie solves 930 math problems in the month of January. How many problems, on average, does she solve each day in that particular month?
5	If $5a + 1 = 15$, then what is the value of $7a$? Express your answer as a common fraction.

6. <u>hours</u>	Darla currently has 22 robots, and s currently has 71 robots, and he destro hours will Darla and Mark have the sa	bys 2 of his robots each hour.	
7	Roland received the following grades 94, 99. What is the sum of the mean, r card? Express your answer as a decim	nedian, and mode of the grades	
8. <u>\$</u>	Pranav has a certain amount of mone quarter of the money on groceries. H on gasoline, and then ends up with exa at the beginning of the day?	e spends two-thirds of the remain	aining money
9 percent	The table shows how many students at Westside Middle School are in a particular club. If each student that is in a club belongs only to that club, then what percent of the students at Westside Middle School are in sports club?		
	CLUBS AT WESTSIDE MIDDLE SCHOOL		
	Club	# Students	
	Math	23	
	Science	44	
	Spelling Bee	13 36	
	Sports Book	19	
	None	135	
	Ttolle	155	

_____ If the sum of the square roots of two numbers is equal to the square root of the sum of the two numbers, what is the product of the two numbers?

10.



16.
If the sum of two numbers is 6 and four times the smaller number subtracted from three times the larger number is 4, what is the positive difference between the squares of the both numbers?

17.
Seven positive integers exist such that the mean of these integers is 8, and the median is 7. What is the greatest possible integer in this set of integers?

18.
If
$$f(x) = x^2 + 5x + 4$$
 and $g(x) = x^2 + 3x - 4$, then what is $\frac{g(f(3))}{f(g(3))}$? Express your answer as a common fraction.

19.
cars

19.
cars to red cars at the dealership is 5:3. A shipment of 24 blue cars to red cars to be 2:1. How many total cars are there after the shipment?

20.
values

How many integer values of x satisfy the equation $\left|\frac{1}{2}x + 4\right| < 6$?

21	Let <i>a</i> , <i>b</i> , and <i>c</i> all be numbers such that the arithmetic mean of <i>a</i> and <i>b</i> is 3, the arithmetic mean of <i>b</i> and <i>c</i> is 9, and the arithmetic mean of <i>a</i> and <i>c</i> is 12. What is the arithmetic mean of <i>a</i> , <i>b</i> , and <i>c</i> ?
22	What is the greatest integer value of <i>n</i> such that <i>n</i> ! is less than $(5n)^2$?
23. <u>ways</u>	How many ways are there to give sixteen gifts to four children, if each child must receive at least two gifts?
24	A rectangle is inscribed inside of a semicircle. The ratio of the shorter side of the rectangle to its longer side is 1:3. What is the ratio of the area of the semicircle to that of the rectangle? Express your answer as a common fraction in terms of π .
25	If <i>x</i> is an integer, what is the sum of the values of <i>x</i> that make $(x^2 - 4x + 5)(x^2 + 6x + 9)$ a prime number?
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Ana and Bobbie each arrive at a party at a random time between 3:00 and 7:00, stay 26. for 5 minutes and then leave. What is the probability that Ana and Bobbie see each other at the party? Express your answer as a common fraction. 27. hours Zara has a house with 4 walls and a ceiling. Alex can paint a wall of Zara's house in 2 hours, and he can paint the ceiling in 3 hours. Beth can paint a wall in $1\frac{1}{2}$ hours, and paint the ceiling in $2\frac{1}{2}$ hours. How long would it take for Alex and Beth to paint Zara's whole house if they both start painting the walls at the same time and then paint the roof when the walls are fully painted? Express your answer as a common fraction. Right triangle XYZ has XZ = 30, as shown below. Points A and B lie on sides XY 28. units² and YZ, respectively. If AX = 17 and BZ = 15, what is the area of triangle XYZ? There are exactly 5 lattice points contained within the graph of $x^2 + y^2 \le 1$. How 29. points many lattice points are contained within the graph of $4(x-5)^2 + 4(y+4)^2 \le 400$? 30. The dartboard shown has a radius of 8 inches and is labeled with point values. Each of the concentric circles has a radius two inches less than the next larger circle. If Bart throws three darts randomly at the target, what is the probability that he earns at least twenty points? Express your answer as a common fraction.